

BEYOND LISP

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MAIN POINTS

- Lisp programs are Lisp data—abstract syntax. Programming languages need functions for their abstraction.
- English is important for its semantics—not its syntax.
- The largest piece of cake—Kleene μ operator
- An elephant never forgets and is faithful.
- Resolution considered harmful.
- Special provers are just strategies—Davis-Putnam
- Programs as logical formulas—Algol 48 and Algol 58

PROGRAMS AS DATA—ABSTRACT SYNTAX

- Sums may be represented as $(+ \ x \ y)$, $x + y$, $3^x 7^y$ and $3^x \times 7^y$
- $issum(exp)$, $s1(exp)$, $s2(exp)$, $mksum(exp1, exp2)$
- Programming languages (even Java and Curl) need abstract syntaxes defined and function in the language to parse abstract syntax.
- Lisp is close to its abstract syntax, but needs it anyway
- Input syntax, print syntax, compute with it syntax. $(+ \times 3)$. *I should have given the list structure.*
- $issubroutine(exp)$, $body(exp)$, $isjavaprogram(exp)$
- <http://www-formal.stanford.edu/jmc/towards.html>

ENGLISH AS A PROGRAMMING LANGUAGE—IT SEMANTICS THAT'S IMPORTANT

- COBOL: add 3 to x, FORTRAN: $x = x + 3$, Algol: $x + 3$; trivial variants
- “the largest piece of cake”, Kleene μ operator
- “I need to be at a meeting in Monterrey, Mexico from September 15 to 17” followed by dialog about details.
- “The U.S. wants Iraq to become a non-aggressive, pro-democracy” —Plan government policy. [to be done with a precise definition of democracy].

INCLUDE LOGICAL SENTENCES IN LISP

- (assert '(on block1 ,x)), (assert '((forall boy)((exists girl (only boy))))))
- Also include a theorem prover-problem solver
- Resolution considered harmful.
- Special provers are just tactics in general provers on subproblems, e.g. Davis-Putnam used when only propositional structure is considered. [confession: I can't do it yet.

ELEPHANT

- Elephants never forget. An elephant is faithful, 100%
- A passenger has a reservation if he has made one and it has not been cancelled. Passengers with reservations should be on the passenger list at flight time.
- A necessary condition for program correctness is that a program fulfill its promises.
- Alas, Elephant 2000 is not ready to be implemented.
- <http://www-formal.stanford.edu/jmc/elephant.htm>

ALGOL 48

If we introduce time explicitly as distinct from the counter, Algolic programs can be written as sets of statements. Here's an Algol 60 program for computing the product of two natural numbers.

```
start :  
    i := n;  
    p := 0;  
loop :    if i = 0 then go to done;  
    i := i - 1;  
    goto loop;  
done :
```

Here's what mathematicians might have written in 19th-century programming languages existed.

```
pc(0) = 0;
i(t + 1) = if pc(t) = 1 then i(t) + 1
else if pc(t) = 4 then i(t) - 1 else i(t);
p(t + 1) = if pc(t) = 2 then p(t) + 1
else if pc(t) = 5 then p(t) + m else p(t);
pc(t + 1) = if pc(t) = 1 then 2
else if pc(t) = 5 then 2 else pc(t) + 1;
```

The proof that $\exists t.(t \geq 0 \wedge pc(t) = 6 \wedge p(t) = mn)$ follows from the sentences expressing the program and the laws of arithmetic, i.e. no theory of program correctness is needed. However, the proof ideas are essentially the same as those used to prove that an algolic program terminates and that the outputs are in a correct relation to the inputs. Amir Pnueli and Nissim G. Zaks had this idea before I did, but they mistakenly abandoned temporal logic.

PROVING LISP PROGRAMS CORRECT